

Please circle your final answers

1. In a particular jurisdiction, license plates consist of any three letters, the first of which cannot be I or O, followed by any three non-repeating digits. Determine the number of possible license plates.

2

2. Consider the letters in the word "REGRETTABLE". Determine the number of possible arrangements if:  
 (a) There are no restrictions

(b) Each arrangement must start with an B

4

(c) Each arrangement must start with an E

(d) Each arrangement must start and end with a T

3. In a particular family of 8 children, there are 5 boys and 3 girls. A photographer is hired to take a series of family pictures of the children only, where they're arranged in a row. How many ways can this be done if:

a) There are no restrictions

b) If the boys must be on the left side, and the girls on the right side, girls on the right:



c) If the girls must all be together

d) If two of the girls, Elizabeth and Katie, **cannot** be together

e) If the photograph consists of just three children – 2 boys and 1 girl. (The photographer selects the three, then arranges them in a row)

5

4. **NR** The three  $\rightarrow$  problems that can be solved using  $\binom{n}{r}$  are \_\_\_\_\_, \_\_\_\_\_, and \_\_\_\_\_

2

5. Algebraically determine the va

- 1 The number of different arrangements using all the letters in the word MATHY
- 2 The number of unique 5 player teams that can be selected from 8 boys and 9 girls
- 3 The number of line segments that can be drawn using the vertices of an 8-sided polygon that are marked on a circle.
- 4 The number of different way to choose 4 specialty donuts from a display of 6 different donuts at a coffee shop
- 5 The number of different ways to assign the job of chairperson, vice-chair, and secretary for a committee from 6 people.

6. Consider the letters in the word SMILE and FROG. The consonants are S, M, L, F, R, and G.
- (a) How many ways can any 2 letters be selected from the word SMILE? (*That is, how many two-letter groups, not arrangements, are possible?*)
  - (b) How many ways can any 2 letters be selected from the word SMILE and any 2 letters be selected from the word FROG?

- (c) How many ways can the letters in any four-letter word be arranged? (*Assuming all letters are different*)
- (d) How many different 4-letter arrangements are possible using any 2 letters from the word SMILE and any 2 letters from the word FROG?

7. A student council consists of 7 girls and 5 boys. A subcommittee of four council members is needed to coordinate a school dance. How many ways can this be done if:
- (a) There are no restrictions

- (b) There must be exactly 2 boys and 2 girls

- (c) There must be exactly 2 boys and 2 girls, and the council president Claire (girl) must be on the subcommittee?

- (d) If either Claire **or** the vice-president David (boy) must on the subcommittee. (Hint: Consider two different cases)

- (e) There must be at least one boy on the subcommittee.

**BONUS:** A pizzeria offers a \$9.99 special, where a medium pizza with up to five toppings can be ordered. (That is, a customer can order less toppings if they wish) Assuming double-toppings are not permitted, a plain cheese pizza counts as no toppings, and there are 12 toppings to choose from, determine the total number of orders possible.